Julia: A Fast Dynamic Language for Technical Computing

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Abstract

Dynamic languages have become popular for scientific computing. They are generally considered highly productive, but lacking in performance. This paper presents Julia, a new dynamic language for technical computing, designed for performance from the beginning by adapting and extending modern programming language techniques. A design based on generic functions and a rich type system simultaneously enables an expressive programming model and successful type inference, leading to good performance for a wide range of programs. This makes it possible for much of Julia’s library to be written in Julia itself, while also incorporating best-of-breed C and Fortran libraries.

1 Introduction

Convenience is winning. Despite advances in compiler technology and execution for high-performance computing, programmers continue to prefer high-level dynamic languages for algorithm development and data analysis in applied math, engineering, and the sciences. High-level environments such as MATLAB®, Octave [26], R [18], SciPy [29], and SciLab [17] provide greatly increased convenience and productivity. However, C and Fortran remain the gold standard languages for computationally-intensive problems because high-level dynamic languages still lack sufficient performance. As a result, the most challenging areas of technical computing have benefited the least from the increased abstraction and productivity offered by higher level languages.

Two-tiered architectures have emerged as the standard compromise between convenience and performance: programmers express high-level logic in a dynamic language while the heavy lifting is done in C and Fortran. The aforementioned dynamic technical computing environments are all themselves instances of this design. While this approach is effective for some applications, there are drawbacks. It would be preferable to write compute-intensive code in a more productive language as well. This is particularly true when developing parallel algorithms, where code complexity can increase dramatically. Instead, there is pressure to write “vectorized” code, which is unnatural for many problems and might generate large temporary objects which could be avoided with explicit loops. Programming in two languages is more complex than using either language by itself due to the need for mediation between

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different type domains and memory management schemes. Interfacing between layers may add significant overhead and makes whole-program optimization difficult. Two-tiered systems also present a social barrier, preventing most users from understanding or contributing to their internals.

An alternative to the two-tier compromise is to enhance the performance of existing dynamic languages. There has been significant progress along these lines. Projects like the Python compiler framework PyPy [6] have been fairly successful. Similar efforts exist for languages from LISP onward. The common feature of all such projects is that they seek to add performance to an existing language. This is obviously useful, since existing code can benefit. While promising, these efforts have yet to eliminate the need for the two-tier approach in practice. Design decisions made under the assumption that a language would be implemented as an interpreter tend to sabotage the ability to generate efficient code. As Henry Baker observed of Common LISP, “...the polymorphic type complexity of the Common LISP library functions is mostly gratuitous, and both the efficiency of compiled code and the efficiency of the programmer could be increased by rationalizing this complexity.” [3] Others have echoed these sentiments [7] [25].

Julia is designed from the ground up to take advantage of modern techniques for executing dynamic languages efficiently. As a result, Julia has the performance of a statically compiled language while providing interactive dynamic behavior and productivity like Python, LISP or Ruby. The key ingredients of performance are:

- Rich type information, provided naturally by multiple dispatch;
- Aggressive code specialization against run-time types;
- JIT compilation using the LLVM compiler framework [21].

Although a sophisticated type system is made available to the programmer, it remains unobtrusive in the sense that one is never required to specify types. Type information flows naturally from having actual values (and hence types) at the time of code generation, and from the language’s core paradigm: by expressing the behavior of functions using multiple dispatch, the programmer unwittingly provides the compiler with extensive type information.

We validate our design by implementing Julia’s standard library, which encompasses most of the core functionality of standard technical computing environments, in Julia itself. As a result, our library code is more generic and compact, and it is possible to inline library code into user code and vice versa. Julia was announced as an open source project in February 2012. New users have been easily able to read the standard library code, modify it, imitate it, and extend it for their own purposes. Our goals and work so far seem to have struck a chord — a significant community has grown around Julia in the short time since the initial public announcement.

## 2 Language Design

Julia’s primary means of abstraction is dynamic multiple dispatch. Much of a language consists of mechanisms for selecting code to run in different situations — from method selection to instruction selection. We use only dynamic multiple dispatch for this purpose, which is possible through sufficiently expressive dispatch rules.
To obtain the desired expressiveness and compile-time type information, we must employ fairly sophisticated types. To balance this requirement with usability, we have attempted to design the “easy version” of key features, namely parametric types and methods. We provide these features without a concept of static application (e.g. template instantiation), without distinct type and expression contexts, and leaving parameters optional whenever possible. Dynamic languages need parametric types so a compiler can keep track of the types of values even when they are stored in shared mutable data structures (optimizing compilers would need this feature even if the types are not exposed in the language as they are in Julia).

Types may be used to make declarations, but we do not require declarations for performance. To achieve this, Julia’s compiler automatically specializes methods for types encountered at run time (or at compile time, to the extent types are known then). Effectively, every method is a template (in the C++ sense) by default, with parameterization and instantiation directed by the compiler. We introduce some type-based heuristics for controlling method specialization.

2.1 Rationale

In past work on optimizing dynamic languages, researchers have observed that programs are not as dynamic as their authors might think: “We found that dynamic features are pervasive throughout the benchmarks and the libraries they include, but that most uses of these features are highly constrained...” [16]. In this sense, the designs of existing dynamic languages do not present a good trade-off. Much code is statically-typeable and could be executed more efficiently, but the language designs and implementations do not anticipate this fact.

We hypothesize that the following forms of “dynamism” are the most useful:

- The ability to run code at load time and compile time, eliminating some of the distractions of build systems and configuration files.
- A universal Any type as the only true static type, allowing the issue of static types to be ignored when desired.
- Never rejecting code that is syntactically well-formed.
- Behavior that depends only on run-time types (i.e. no static overloading).

Julia avoids some of the “overly permissive” features of systems like CLOS [4] that get in the way of compiler optimizations, using the following restrictions:

- Types themselves are immutable.
- The type of a value cannot change over its lifetime.
- Local variable environments are not reified.
- Program code is immutable (but new code may be generated and executed at any time).
- Not all bindings are mutable (const identifiers are allowed).

These restrictions allow the compiler to see all uses of local variables, and perform dataflow analysis on local variables using only local information. This is important, since it allows user code to call statically-unknown functions without interfering with optimizations done around such call sites. Statically-unknown function calls arise in many contexts, such as calling a function taken from an untyped data structure, or dynamically dispatching a method call due to unknown argument types.
2.2 Core Language Overview

The core Julia language contains the following components:

1. A syntax layer, to translate surface syntax to a suitable intermediate representation (IR).
2. A symbolic language and corresponding data structures for representing certain kinds of types, and implementations of lattice operators (meet, join, and ≤) for those types.
3. An implementation of generic functions and dynamic multiple dispatch based on those types.
4. Compiler intrinsic functions for accessing the object model (type definition, method definition, object allocation, element access, testing object identity, and accessing type tags).
5. Compiler intrinsic functions for native arithmetic, bit string operations, and calling native (C or Fortran) functions.
6. A mechanism for binding top-level names.

The IR describes a function body as a sequence of assignment operations, function calls, labels, and conditional branches. Julia’s semantics are those of a standard imperative language: statements are executed in order, with function arguments evaluated eagerly. All values are conceptually references, and are passed by reference as in LISP.

2.3 Types

Julia treats types as symbolic descriptions of sets of values. Every value has a unique, immutable, run-time implementation type. Objects carry type tags, and types themselves are Julia objects that can be created and inspected at run time. Julia has five kinds of types:

1. Abstract types, which may have declared subtypes and supertypes (a subtype relation is declared using the notation Sub <: Super)
2. Composite types (similar to C structs\(^1\)), which have named fields and declared supertypes
3. Bits types, whose values are represented as bit strings, and which have declared supertypes
4. Tuples, immutable ordered collections of values
5. Union types, abstract types constructed from other types via set union

Bits types allow users to add new fixed-width number-like types and obtain the same performance that primitive numeric types enjoy in other systems. Julia’s “built in” numeric types are defined as bits types. Julia method dispatch is based on types rather than field lookup, so whether a value is of a bits type or composite type is a representation detail that is generally invisible.

\(^1\)Currently, composite types are mutable, but we plan to make mutability optional.
Tuples are used to represent the types of method arguments and multiple return values. The type of a tuple is defined recursively as a tuple of the types of its elements. Tuple types are covariant; a tuple type is a subtype of another if its elements are subtypes of the corresponding elements of the other. Tuple types may end in a special ... type that indicates any number of elements may be added. This is used to express the types of variadic methods. For example the type \(\text{Tuple}(\text{String}, \text{Int}...)\) indicates a tuple where the first element is a String and any number of trailing integers may be present.

Union types are used primarily to construct tight least upper bounds when the inference algorithm needs to join unrelated types. For example, a method might return an \(\text{Int}\) or a \(\text{String}\) in separate arms of a conditional. In this case its type can be inferred as \(\text{Union}(\text{Int}, \text{String})\). Union types are also useful for defining ad-hoc type hierarchies different from those imagined when the types involved were first defined. Lastly, union types can be used to declare methods applicable to multiple types.

### 2.4 Type Parameters

Abstract types, composite types, and bits types may have parameters, which makes it possible to express variants of a given type (for example, array types with different element types). These types are all invariant with respect to their parameters (i.e. two versions of the same type with different parameters are simply different, and have no subtype relationship). Type constructors are applied using curly braces, as in \(\text{Array}(\text{Float64}, 1)\) (the \(\text{Array}\) type is parameterized by element type and rank). Semantically, a type constructor application is a function call expression evaluated at run time.

Type parameters may have bounds [8], also declared using the \(\ll\) operator, as in \(\text{Rational}\{T<:\text{Integer}\}\).

To help meet our goal of convenience, we allow writing parametric types without parameters, or omitting trailing parameters. \(\text{Array}\) refers to any kind of dense array, and \(\text{Array}(\text{Float64})\) refers to a Float64 Array of any rank. The result of one of these expressions is effectively an ad-hoc abstract supertype of all instantiations one could obtain by filling in the missing parameters.

This design also makes it easy to add parameters to types later; existing code does not need to be modified.

### 2.5 Generic Functions

The vast majority of Julia functions (in both the library and user programs) are generic functions, meaning they contain multiple definitions or methods for various combinations of argument types. When a generic function is applied, the most specific definition that matches the run-time argument types is invoked. Generic functions have appeared in several object systems in the past, notably CLOS [15] and Dylan [28]. Julia is distinguished from these in that it uses generic functions as its primary abstraction mechanism, putting it in the company of research languages like Diesel [10] and Cecil [9]. Aside from being practical for mathematical styles of programming, this design is satisfying also because it permits expression of most of the popular patterns of object-oriented programming, while leaving the core language with fewer distinct features.
2.6 Method Definition

Method definitions have a long (multi-line) form and a short form.

```julia
function iszero(x::Number)
    return x==0
end

iszero(x) = (x==0)
```

A type declaration with :: on an argument is a dispatch specification. When types are omitted, the default is Any. A :: expression may be added to any program expression, in which case it acts as a run-time type assertion. As a special case, when :: is applied to a variable name in statement position (a construct which otherwise has no effect) it means the variable always has the specified type, and values will be converted to that type (by calling convert) on assignment to the variable.

Note that there is no distinct type context; types are computed by ordinary expressions evaluated at run time. For example, f(x)::Int is lowered to the function call typeassert(f(x),Int).

Anonymous functions are written using the syntax x->x+1.

Local variables are introduced implicitly by assignment. Modifying a global variable requires a global declaration.

Operators are simply functions with special calling syntax. Their definitions look the same as those of ordinary functions, for example +(x,y) = ... , or function +(x,y).

When the last argument in a method signature is followed by ... the method accepts any number of arguments, and the last argument name is bound to a tuple containing the tail of the argument list. The syntax f(t...) "splices" the contents of an iterable object t as the arguments to f.

Generic functions are a natural fit for mathematical programming. For example, consider implementing exponentiation (the ^ operator in Julia). This function lends itself to multiple definitions, specializing on both arguments separately: there might be one definition for two floating-point numbers that calls a standard math library routine, one definition for the case where the second argument is an integer, and separate definitions for the case where the first argument is a matrix. In Julia these signatures would be written as follows:

```julia
function ^(x::Float64, p::Float64)
function ^(x, p::Int)
function ^(x::Matrix, p)
```

2.7 Parametric Methods

It is often useful to refer to parameters of argument types inside methods, and to specify constraints on those parameters for dispatch purposes. Method parameters address these needs. These parameters behave a bit like arguments, but they are always derived automatically from method argument types and not specified explicitly by the caller. The following signature presents a typical example:

```julia
function assign{T<:Integer}(a::Array{T,1}, i, n::T)
```
This signature is applicable to 1-dimensional arrays whose element type is some kind of integer, any type of second argument, and a third argument that is the same type as the array’s element type. Inside the method, T will be bound to the array element type.

The primary use of this construct is to write methods applicable to a family of parametric types (e.g. all integer arrays, or all numeric arrays) despite invariance. The other use is writing “diagonal” constraints as in the example above. Such diagonal constraints significantly complicate the type lattice operators.

2.8 Constructors

Composite types are applied as functions to construct instances. The default constructor accepts values for each field as arguments. Users may override the default constructor by writing method definitions with the same name as the type inside the type definition block. Inside the type block the identifier new is bound to a pseudofunction that actually constructs instances from field values. The constructor for the Rational type is a good example:

```plaintext
type Rational{T<:Integer} <: Real
  num::T
  den::T

  function Rational(num::T, den::T)
    if num == 0 && den == 0
      error("invalid rational: 0//0")
    end
    g = gcd(den, num)
    new(div(num, g), div(den, g))
  end
end
```

This allows Rational to enforce representation as a fraction in lowest terms.

2.9 Singleton Kinds

A generic function’s method table is effectively a dictionary where the keys are types. This suggests that it should be just as easy to define or look up methods with types themselves as with the types of values. Defining methods on types directly is analogous to defining class methods in class-based object systems. With multi-methods, definitions can be associated with combinations of types, making it easy to represent properties not naturally owned by one type.

To accomplish this, we introduce a special singleton kind Type{T}, which contains the type T as its only value. The result is a feature similar to eql specializers in CLOS, except only for types. An example use is defining type traits:

```plaintext
typemax(::Type{Int64}) = 9223372036854775807
```

This definition will be invoked by the call typemax(Int64). Note that the name of a method argument can be omitted if it is not referenced.
Types are useful as method arguments in several other cases. One example is file I/O, where a type can be used to specify what to read. The call `read(file, Int32)` reads a 4-byte integer and returns it as an `Int32` (a fact that the type inference process is able to discover). We find this more elegant and convenient than systems where enums or special constants must be used for this purpose, or where the type information is implicit (e.g. through return-type overloading).

This feature allows sharper types to be inferred when the user programs with types, for example by calling the `typeof` function or applying type constructors. As a result, we gain the performance and flexibility advantages of static parameters (such as template arguments) without special syntax.

2.10 Method Sorting and Ambiguity

Methods are stored sorted by specificity, so the first matching method (as determined by the subtype predicate) is always the correct one to invoke. This means much of the dispatch logic is contained in the sorting process. Comparing method signatures for specificity is not trivial. As one might expect, the “more specific”\(^2\) predicate is quite similar to the subtype predicate, since a type that is a subtype of another is indeed more specific than it. However, a few additional rules are necessary to capture the intuitive concept of “more specific”. Our formal definition is summarized as the disjunction of the following rules (\(A\) is more specific than \(B\) if):

1. \(A\) is a subtype of \(B\)
2. \(A\) is of the form \(T\{P\}\) and \(B\) is of the form \(S\{Q\}\), and \(T\) is a subtype of \(S\) for some parameter values
3. The intersection of \(A\) and \(B\) is nonempty, more specific than \(B\), and not equal to \(B\), and \(B\) is not more specific than \(A\)
4. \(A\) and \(B\) are tuple types, \(A\) ends in a vararg (\(\ldots\)) type, and \(A\) would be more specific than \(B\) if its vararg type were expanded to give it the same number of elements as \(B\)
5. \(A\) and \(B\) have parameters and compatible structures, and \(A\) provides a consistent assignment for \(B\)’s parameters, but not the other way around

Rule 2 means that declared subtypes are always more specific than their declared supertypes regardless of type parameters. Rule 3 is mostly useful for union types: if \(A\) is `Union(Int32, String)` and \(B\) is `Number`, \(A\) should be more specific than \(B\) because their intersection (\(Int32\)) is clearly more specific than \(B\). Rule 4 means that argument types are more important for specificity than argument count; if \(A\) is `(Int32...)` and \(B\) is `(Number, Number)` then \(A\) is more specific.

Rule 5 makes diagonal constraints more specific; \(\forall T(T, T)\) is more specific than \(\forall X, Y(X, Y)\). The specificity of a type variable is determined extensionally, i.e. according to the set of values it would ultimately encompass. For example, \(T <: Number\) has the same specificity as `Number`. This approach has been found useful in past work combining parametric types and multiple dispatch [1].

\(^2\)Actually, “not less specific”, since specificity is a partial order.
Julia uses symmetric multiple dispatch, which means all arguments are equally important. Therefore, ambiguous signatures are possible. For example, given `foo(x::Number, y::Int)` and `foo(x::Int, y::Number)` it is not clear which method to call when both arguments are integers. We detect ambiguities when a method is added, by looking for a pair of signatures with a non-empty intersection where neither one is more specific than the other. A warning message is displayed for each ambiguity, showing the user the computed type intersection so it is clear what definition is missing. For example:

```
Warning: New definition foo(Int,Number) is ambiguous with foo(Number,Int). Make sure foo(Int,Int) is defined first.
```

### 2.11 Iteration

A `for` loop is translated to a while loop with method calls according to an iteration interface (`start, done, and next`).

```python
for i in range
    # body
end
```

Becomes:

```python
state = start(range)
while !done(range, state)
    (i, state) = next(range, state)
    # body
end
```

This design for iteration was chosen because it is not tied to mutable heap-allocated state, such as an iterator object that updates itself.

### 2.12 Special Operators

Special syntax is provided for certain functions.

<table>
<thead>
<tr>
<th>surface syntax</th>
<th>lowered form</th>
</tr>
</thead>
<tbody>
<tr>
<td>a[i, j]</td>
<td>ref(a, i, j)</td>
</tr>
<tr>
<td>a[i, j] = x</td>
<td>assign(a, x, i, j)</td>
</tr>
<tr>
<td>[a; b]</td>
<td>vcat(a, b)</td>
</tr>
<tr>
<td>[a, b]</td>
<td>vcat(a, b)</td>
</tr>
<tr>
<td>[a b]</td>
<td>hcat(a, b)</td>
</tr>
<tr>
<td>[a b; c d]</td>
<td>hvcat((2,2), a, b, c, d)</td>
</tr>
</tbody>
</table>

### 2.13 Calling C and Fortran

We provide the keyword `ccall` for calling native code in-line. Its syntax looks like a function call, where the programmer specifies an address, result and argument types, and argument values:
The first three arguments to `ccall` are actually pseudo-arguments, evaluated at compile time. The compiler front-end inserts calls to the `convert` function for each argument, ensuring that the actual arguments will match the provided signature.

In Fortran, all arguments are passed by reference. To handle this, argument types must be written as pointer types such as `Ptr{Float64}`. An ambiguity then arises in argument conversion: an integer argument could be interpreted as a pointer, or as a number to convert to `Float64` and pass by reference. To resolve this ambiguity, the programmer can request the second interpretation by prefixing an argument with an ampersand (a pun on C syntax for taking the address of a value), as in `&x`.

### 2.14 Parallelism

Parallel execution is provided by a message-based multi-processing system implemented in Julia in the standard library. The language design supports the implementation of such libraries by providing symmetric coroutines, which can also be thought of as cooperatively scheduled threads. This feature allows asynchronous communication to be hidden inside libraries, rather than requiring the user to set up callbacks. Julia does not currently support native threads, which is a limitation, but has the advantage of avoiding the complexities of synchronized use of shared memory.

### 2.15 Design Limitations

In our design, type information always flows along with values, in the forward control flow direction. This prevents us from doing certain tricks that static type systems are capable of, such as return-type overloading. Return-type overloading requires a robust notion of the type of a value _context_—the type expected or required of some term—in order to select code on that basis. There are other cases where “backwards” type flow might be desirable, such as determining the type of a container based on the type of a value stored into it at a later program point. It may be possible to get around this limitation in the future using inversion of control—passing a function argument whose result type has already been inferred, and using that type to construct a container before elements are computed.

Modularity is a perennial difficulty with multiple dispatch, as any function might apply to any type, and there is no point where functions or types are closed to future definitions. Thus at the moment Julia is essentially a whole-program compiler. We plan to implement a module system that will at least allow code to control which name bindings and definitions it sees. Such modules could be separately compiled to the extent that programmers are willing to ask for their definitions to be “closed”.

Lastly, at this time Julia uses a bit more memory than we would prefer. Our compiler data structures, type information, and generated native code take up more space than the compact bytecode representations used by many dynamic languages.

### 3 Implementation

Much of the implementation is organized around method dispatch. The dispatch logic is both a large portion of the behavior of Julia functions, and the entry point of the compiler’s type inference and specialization logic.
3.1 Method Caching and Specialization

The first step of method dispatch is to look for the argument types in a per-function cache. The cache has an entry for (almost) every set of concrete types to which the function has been applied. Concrete types are hash-consed, so they can be compared by simple pointer comparison. This makes cache lookup faster than the `subtype` predicate. As part of hash-consing, concrete types are assigned small integer IDs. The ID of the first argument is used as a primary key into a method cache, so when signatures differ only in the type of the first argument a simple indexed lookup suffices.

On a cache miss, a slower search for the matching definition is performed using `subtype`. Then, type inference is invoked on the matching method using the types of the actual arguments. The resulting type-annotated and optimized method is stored in the cache. In this way, method dispatch is the primary source of type information for the compiler.

3.2 Method Specialization Heuristics

Our aggressive use of code specialization has the obvious pitfall that it might lead to excessive code generation, consuming memory and compile time. We found that a few mild heuristics suffice to give a usable system with reasonable resource requirements.

The first order of business is to ensure that the dispatch and specialization process converges. The reason it might not is that our type inference algorithm is implemented in Julia itself. Calling a method on a certain type \( A \) can cause the type inference code to call the same method on type \( B \), where types \( A \) and \( B \) follow an infinite ascending chain in either of two partial orders (the `typeof` order or the `subtype` order). Singleton kinds are the most prominent example, as type inference might attempt to successively consider `Int32`, `Type{Int32}`, `Type{Type{Int32}}`, and so on. We stop this process by replacing any nestings of `Type` with the unspecialized version of `Type` during method specialization (unless the original method declaration actually specified a type like `Type{Type{Int32}}`).

The next heuristic avoids specializing methods for tuple types of every length. Tuple types are cached as the intersection of the declared type of the method slot with the generic tuple type `(Any...)`. This makes the resulting cache entry valid for any tuple argument, again unless the method declaration contained a more specific tuple type. Note that all of these heuristics require corresponding changes in the method cache lookup procedure, since they yield cache entries that do not have to exactly match candidate arguments.

A similar heuristic is applied to variadic methods, where we wish to avoid caching argument lists of every length. This is done by capping argument lists at the length of the longest signature of any method in the same generic function. The “capping” involves replacing the last argument with a `...` type. Ideally, we want to form the biggest type that’s not a supertype of any other method signatures. However, this is not always possible and the capped type might conflict with another signature. To deal with this case, we find all non-empty intersections of the capped type with other signatures, and add dummy cache entries for them. Hitting one of these entries alerts the system that the arguments under consideration are not really in the cache. Without the dummy entries, some arguments might incorrectly match the capped type, causing the wrong method to be invoked.

The next heuristic concerns singleton kinds again. Because of the singleton kind feature, every distinct type object (`Any`, `Number`, `Int`, etc.) passed to a method might trigger a new specialization. However, most methods are not “class methods” and are not concerned with
type objects. Therefore, if no method definition in a certain function involves Type for a certain argument slot, then that slot is not specialized for different type objects.

Finally, we introduce a special type ANY that can be used in a method signature to hint that a slot should not be specialized. This is used in the standard library in a small handful of places, and in practice is less important than the heuristics described above.

### 3.3 Type Inference

Types of program expressions and variables are inferred by forward dataflow analysis\(^3\). The original algorithm for such dynamic type inference was given by Kaplan and Ullman [20]. This is different from type inference in the ML family of languages [27], where the compiler must be able to determine types, using an algorithm based on unification. Dynamic type inference has been applied to LISP [23] [5] [3], and object-oriented languages such as Self [11] and JavaScript [2].

We determine a maximum fixed-point (MFP) solution using Algorithm 1, based on Mohnen’s graph-free dataflow analysis framework [24]. The basic idea is to keep track of the state (the types of all variables) at each program point, determine the effect of each statement on the state, and ensure that type information from each statement eventually propagates to all other statements reachable by control flow. We augment the basic algorithm with support for mutually-recursive functions (functions are treated as program points that might need to be revisited).

The origin of the type information used by the MFP algorithm is evaluation of known functions over the type domain [12]. This is done by the eval subroutine. The interpret subroutine calls eval, and also handles assignment statements by returning the new types of affected variables. Each known function call is either to one of the small number of built-in functions, in which case the result type is computed by a (usually trivial) hand-written type transfer function, or to a generic function, in which case the result type is computed by recursively invoking type inference. In the generic function case, the inferred argument types are met (\(\sqcap\)) with the signatures of each method definition. Matching methods are those where the meet (greatest lower bound) is not equal to the bottom type (None in Julia). Type inference is invoked on each matching method, and the results are joined (\(\sqcup\)) together. The following equation summarizes this process:

\[
T(f, t_{\text{arg}}) = \bigcup_{(s, g) \in f} T(g, t_{\text{arg}} \sqcap s)
\]

\(T\) is the type inference function. \(t_{\text{arg}}\) is the inferred argument tuple type. The tuples \((s, g)\) represent the signatures \(s\) and their associated definitions \(g\) within generic function \(f\).

Two optimizations are helpful here. First, it is rarely necessary to consider all method definitions. Since methods are stored in sorted order, as soon as the union of the signatures considered so far is a supertype of \(t_{\text{arg}}\), no more definitions need to be considered. Second, the join operator employs widening [13]: if a type becomes too large it may simply return \textit{Any}. In this case the recursive inference process may stop immediately.

\(^3\)Adding a reverse dataflow pass could potentially improve type information, but we have not yet done this.
Algorithm 1 Infer function return type

**Require:** function \( F \), argument type tuple \( A \), abstract execution stack \( S \)

**Ensure:** result type \( S.R \)

\[
\begin{align*}
V & \leftarrow \text{set of all locally-bound names} \\
V_a & \leftarrow \text{argument names} \\
n & \leftarrow \text{length}(F) \\
W & \leftarrow \{1\} \{\text{set of program counters}\} \\
P_r & \leftarrow \emptyset \{\text{statements that recur}\} \\
\forall v \in V, \Gamma[1][v] & \leftarrow \text{Undef} \\
\forall i, \Gamma[1][V_a[i]] & \leftarrow A[i] \{\text{type environment for statement } 1\} \\
\text{while } W \neq \emptyset \text{ do} \\
\quad p & \leftarrow \text{choose}(W) \\
\quad \text{repeat} \\
\quad \\
\quad W & \leftarrow W - p \\
\quad \text{new} & \leftarrow \text{interpret}(F[p], \Gamma[p], S) \\
\quad \text{if } S.rec \text{ then} \\
\quad \\
\quad P_r & \leftarrow P_r \cup \{p\} \\
\quad S.rec & \leftarrow \text{false} \\
\quad \text{end if} \\
\quad p' & \leftarrow p + 1 \\
\quad \text{if } F[p] = (\text{goto l}) \text{ then} \\
\quad \\
\quad p' & \leftarrow l \\
\quad \text{else if } F[p] = (\text{gotoif cond l}) \text{ then} \\
\quad \\
\quad \text{if not } \text{new} \leq \Gamma[l] \text{ then} \\
\quad \\
\quad W & \leftarrow W \cup \{l\} \\
\quad \Gamma[l] & \leftarrow \Gamma[l] \sqcup \text{new} \\
\quad \text{end if} \\
\quad \text{else if } F[p] = (\text{return e}) \text{ then} \\
\quad \\
\quad p' & \leftarrow n + 1 \\
\quad r & \leftarrow \text{eval}(e, \Gamma[p], S) \\
\quad \text{if not } r \leq S.R \text{ then} \\
\quad \\
\quad S.R & \leftarrow S.R \sqcup r \\
\quad W & \leftarrow W \cup P_r \\
\quad \text{end if} \\
\quad \text{end if} \\
\quad \text{if } p' \leq n \text{ and not } \text{new} \leq \Gamma[p'] \text{ then} \\
\quad \\
\quad \Gamma[p'] & \leftarrow \Gamma[p'] \sqcup \text{new} \\
\quad p & \leftarrow p' \\
\quad \text{end if} \\
\quad \text{until } p' = n + 1 \\
\text{end while} \\
S.rec & \leftarrow P_r \neq \emptyset
\end{align*}
\]
3.3.1 Interprocedural Type Inference

Type inference is invoked through “driver” Algorithm 2 which manages mutual recursion and memoization of inference results. A stack of abstract activation records is maintained and used to detect recursion. Each function has a property \textit{incomplete}(F, A) indicating that it needs to be revisited when new information is discovered about the result types of functions it calls. The \textit{incomplete} flags collectively represent a set analogous to \( W \) in Algorithm 1.

The outer loop in Algorithm 2 looks for an existing activation record for its input function and argument types. If one is found, it marks all records from that point to the top of the stack, identifying all functions involved in the call cycle. These marks are discovered in Algorithm 1 when \textit{interpret} returns, and all affected functions are considered \textit{incomplete}. Algorithm 2 continues to re-run inference on incomplete functions, updating the inferred result type, until no recursion occurs or the result type converges.

\begin{algorithm}
\caption{Interprocedural type inference}
\begin{algorithmic}
\Require function \( F \), argument type tuple \( A \), abstract execution stack \( S \)
\Ensure returned result type
\State \( R \leftarrow \bot \)
\If {\text{recall}(F, A) exists}
\State \( R \leftarrow \text{recall}(F, A) \)
\If {\text{not} \text{incomplete}(F, A)}
\State \text{return} \( R \)
\EndIf
\EndIf
\State \( f \leftarrow S \)
\While {\text{not} \text{empty}(f)}
\If {\( f.F \) is \( F \) and \( f.A = A \)}
\State \( r \leftarrow S \)
\While {\text{not} \( r = \text{tail}(f) \)}
\State \( r.rec \leftarrow \text{true} \)
\State \( r \leftarrow \text{tail}(r) \)
\EndWhile
\State \text{return} \( f.R \)
\EndIf
\State \( f \leftarrow \text{tail}(f) \)
\EndWhile
\State \( S' \leftarrow \text{extend}(S, \text{Frame}(F, A, R, \text{rec} = \text{false})) \)
\EndIf
\EndWhile
\State \text{invoke Algorithm 1 on} \( F, A, S' \)
\State \text{recall}(F, A) \leftarrow S'.R
\State \text{incomplete}(F, A) \leftarrow (S'.rec \land \neg (R = S'.R))
\State \text{return} \( S'.R \)
\end{algorithmic}
\end{algorithm}

3.4 Lattice Operators

Our type lattice is complicated by the presence of type parameters, unions, and diagonal type constraints in method signatures. Fortunately, for our purposes only the \( \leq \) (\textit{subtype}) relation needs to be computed accurately, as it bears final responsibility for whether a method
is applicable to given arguments. Type union and intersection, used to estimate least upper bounds and greatest lower bounds, respectively, may both be conservatively approximated. If their results are too coarse, the worst that can happen is performing method dispatch or type checks at run time, since the inference process will simply conclude that it does not know precise types.

A complication arises from the fact that our abstract domain is available in a first-class fashion to user programs. When a program contains a type-valued expression, we want to know which type it will evaluate to, but this is not possible in general. Therefore in addition to the usual type imprecision (not knowing the type of a value), we must also model type uncertainty, where a type itself is known imprecisely. A common example is application of the typeof primitive to a value of imprecise type. What is the abstract result of typeof(x::Number)?

We handle this using bounded type variables, effectively representing a range rather than a point within the type lattice. In this example, the transfer function for typeof is allowed to return Type{T<:Number}, where T is a new type variable.

3.4.1 Subtype Predicate

See Algorithm 3. Note that extensional type equality can be computed as $(A \leq B \land B \leq A)$, and this is used for types in invariant context (i.e., type parameters). The algorithm uses subroutines $p(A)$ which gives the parameters of type $A$, and $super(A)$ which gives the declared supertype of $A$.

3.4.2 Type Union

Since our type system directly supports unions, the union of $T$ and $S$ can be computed simply by constructing the type $\text{Union}(T,S)$. An obvious simplification is performed: if one of $T$ or $S$ is a subtype of the other, it can be removed from the union. Nested union types are flattened, followed by pairwise simplification.

3.4.3 Type Intersection

This is the difficult one: given types $T$ and $S$, we must try to compute the smallest type $R$ such that $\forall s, s \in T \land s \in S \Rightarrow s \in R$. The conservative solution is to give up on finding the smallest such type, and return some type with this property. Simply returning $T$ or $S$ suffices for correctness, but in practice this algorithm makes the type inference process nearly useless. A slightly better algorithm is to check whether one argument is a subtype of the other, and return the smaller type. It is also possible to determine quickly, in many cases, that two types are disjoint, and return $\perp$. With these two enhancements we start to obtain some useful type information. However, we need to do better to take full advantage of the framework set up so far.

Our algorithm has two phases. First, the structures of the two input types are analyzed in a manner similar to subtype, except a constraint environment is built, with entries $T \leq S$ for type variables $T$ in covariant contexts (tuples) and entries $T = S$ for type variables $T$ in invariant contexts (type parameters). In the second phase the constraints are solved with an algorithm similar to that used by traditional polymorphic type systems [27].

The code for handling tuples and union types is similar to that in Algorithm 3, so we focus instead on intersecting types in the nominal hierarchy (Algorithm 4). The base case occurs when the input types are from the same family, i.e., have the same typename. All we
Algorithm 3 Subtype

Require: types $A$ and $B$

Ensure: $A \leq B$

if $A$ is a tuple type then
  if $B$ is not a tuple type then
    return false
  end if
  for $i = 1$ to $\text{length}(A)$ do
    if $A[i]$ is $T\ldots$ then
      if last($B$) exists and is not $S\ldots$ then
        return false
      end if
      return $\text{subtype}(T, B[j]), i \leq j \leq \text{length}(B)$
    else if $i > \text{length}(B)$ or not $\text{subtype}(A[i], B[i])$ then
      return false
    else if $B[i]$ is $T\ldots$ then
      return $\text{subtype}(A[j], T)), i < j \leq \text{length}(A)$
    end if
  end for
else if $A$ is a union type then
  return $\forall t \in A, \text{subtype}(t, B)$
else if $B$ is a union type then
  return $\exists t \in B, \text{subtype}(A, t)$
end if
while $A \neq \text{Any}$ do
  if $\text{typename}(A) = \text{typename}(B)$ then
    return $\text{subtype}(\forall p(A), p(B)) \land \text{subtype}(p(B), p(A))$
  end if
  $A \leftarrow \text{super}(A)$
end while
if $A$ is of the form $\text{Type}\{T\}$ then
  return $\text{subtype}$(typeof($p(A)[1])], $B$)
else if $B$ is of the form $\text{Type}\{T\}$ then
  $B \leftarrow p(B)[1]$
  return $\text{subtype}(A, B) \land \text{subtype}(B, A)$
end if
return $B = \text{Any}$
need to do is visit each parameter to collect any needed constraints, and otherwise check that the parameters are equal. When a parameter is a type variable, it is effectively covariant, and must be intersected with the corresponding parameter of the other type to form the final result.

**Algorithm 4** Intersection of nominal types

**Require:** types $A$ and $B$, current constraint environment

**Ensure:** return $T$ such that $A \cap B \leq T$, updated environment

```java
if typename(A) = typename(B) then
    pa ← copy(p(A))
    for $i = 1$ to length(p(A)) do
        if $p(A)[i]$ is a typevar then
            add $(p(A)[i] = p(B)[i])$ to constraints
        else if $p(B)[i]$ is a typevar then
            add $(p(B)[i] = p(A)[i])$ to constraints
        end if
        pa[i] ← intersect(p(A)[i], p(B)[i])
    end for
    return typename(A){pa...}
else
    sup ← intersect(super(A), B)
    if sup = ⊥ then
        sup ← intersect(A, super(B))
        if sup = ⊥ then
            return ⊥
        else
            sub ← B
        end if
    else
        sub ← A
    end if
    E ← conform(sup, super_decl(sub))
    if $E$ contains parameters not in formals(sub) then
        return ⊥
    end if
    return intersect(sub, typename(sub){E...})
end if
```

When the argument types are not from the same family, we recur up the type hierarchy to see if any supertype of one of the arguments matches the other. If so, the recursion gives us the intersected supertype $sup$, and we face the problem of mapping it to the family of the original argument type. To do this, we first call subroutine $conform$, which takes two types with the same structure and returns an environment $E$ mapping any type variables in one to their corresponding components in the other. $super_decl(t)$ returns the type template used by $t$ to instantiate its supertype. If all goes well, this tells us what parameters $sub$ would have to be instantiated with to have supertype $sup$. If, however, $E$ contains type variables not controlled by $sub$, then there is no way a type like $sub$ could have the required supertype,
and the overall answer is \( \bot \). Finally, we apply the base case to intersect \( \text{sub} \) with the type obtained by instantiating its family with parameter values in \( E \).

We use a simple algorithm to solve the type parameter constraints. Constraints \( T \leq S \) where \( S \) is a concrete type are converted to \( T = S \) to help sharpen the result type. If there are any conflicting constraints (\( T = S \) and \( T = U \) where \( S \neq U \)), the type intersection is empty. If each type variable has exactly one constraint \( T = U \), we can substitute \( \text{find}(X, U) \) for each occurrence of \( T \) in the computed type intersection, and we have a final answer. \( \text{find} \) works in the \( \text{union-find} \) sense, following chains of equalities until we hit a non-variable or an unconstrained variable. Unconstrained type variables may be left in place.

The remaining case is type variables with multiple constraints. Finding a satisfying assignment requires intersecting all the upper bounds for a variable. It is here that we choose to throw in the towel and switch to a coarser notion of intersection, denoted by \( \sqcap^* \). Intersection is effectively the inner loop of type inference, so in the interest of getting a reasonable answer quickly we might pick \( X \sqcap^* Y = X \). A few simple heuristics might as well be added; for example cases like two non-parameterized types where one is an immediate subtype of the other can be supported easily.

In our implementation, type intersection handles most of the complexity surrounding type variables and parametric methods. It is used to test applicability of parametric methods; since all run-time argument lists are of concrete type, intersecting their types with method signatures behaves like \( \text{subtype} \), except static parameters are also properly matched. If intersection returns \( \bot \) or does not find values for all static parameters for a method, the method is not applicable. Therefore in practice we do not really have the freedom to implement \( \sqcap \) and \( \sqcap^* \) any way that obeys our correctness property. They must be at least as accurate as \( \text{subtype} \) in the case where one argument is concrete.

### 3.4.4 Widening Operators

Lattices used in practical program analyses often fail to obey the finite chain condition necessary for the MFP algorithm to converge (i.e. they are not of finite height) and ours is no exception.

Widening is applied in two places: by the join operator, and on every recursive invocation of type inference. When a union type becomes too large (as determined by a cutoff), it is replaced with \( \text{Any} \). Tuple types lend themselves to two infinite chains: one in depth (\( (\text{Any},), \), \( (\text{Any},),, \), etc.) and one in length (\( (\text{Any}...,), (\text{Any},\text{Any}...,), (\text{Any},\text{Any},\text{Any}...,), \) etc.). These chains are capped at arbitrary cutoffs each time the inference process needs to construct a tuple type.

### 3.5 Code Generation and Optimization

After type inference is complete, we annotate each expression with its inferred type. We then run two key optimization passes. If the inferred argument types in a method call indicate that a single method matches, we are free to inline that method. For methods that return multiple values, inlining often yields expressions that construct tuples and immediately take them apart. The next optimization pass identifies these cases and removes the tuple allocations.

The next set of optimizations is applied during code generation. Our code generator targets the LLVM compiler framework [21]. First, we examine uses of variables and assign local variables specific scalar types where possible (LLVM uses a typed code representation).
The box operations used to tag bit strings with types are done lazily; they add a compile-time tag that causes generation of the appropriate allocation code only when the value in question hits a context that requires it (for example, assignment to an untyped data structure, or being passed to an unknown function).

The code generator recognizes calls to key built-in and intrinsic functions, and replaces them with efficient in-line code where possible. For example, the `is` function on mutable arguments yields a pointer comparison, and `typeof` might yield a constant pointer value if the type of its argument is known. Calls known to match single methods generate code to call the correct method directly, skipping the dispatch process.

Finally, we run several of LLVM’s optimization passes. This provides standard scalar optimizations, such as strength reduction, dead code elimination, jump threading, and constant folding.

4 Example Use Cases

4.1 Numeric Type Promotion

Numeric types and arithmetic are fundamental to all programming, but deserve extra attention in the case of scientific computing. In traditional compiled languages such as C, the arithmetic operators are the most polymorphic “functions”, and hence cannot be written in the language itself. Arithmetic must be defined in the compiler, including contentious decisions such as how to handle operations with mixed argument types.

In Julia, multiple dispatch is used to define arithmetic and type promotion behaviors at the library level rather than in the compiler. As a result, the system smoothly incorporates new operators and numeric types with minimal work.

Four key utility functions comprise the type promotion system. For simplicity, we consider only two-argument forms of promotion although multi-argument promotion is also defined and used.

1. `convert(T, value)` converts its second argument to type $T$

2. `promote_rule(T1,T2)` defines which of two types is greater in the promotion partial order

3. `promote_type(T1,T2)` uses `promote_rule` to determine which type should be used for values of types $T1$ and $T2$

4. `promote(v1, v2)` converts its arguments to an appropriate type and returns the results

`promote` is implemented as follows:

```plaintext
function promote{T,S}(x::T, y::S)
    (convert(promote_type(T,S),x),
    convert(promote_type(T,S),y))
end
```

`promote_type` simply tries `promote_rule` with its arguments in both orders, to avoid the need for repeated definitions:
function promote_type{T,S}(::Type{T}, ::Type{S})
if applicable(promote_rule, T, S)
    return promote_rule(T,S)
elseif applicable(promote_rule, S, T)
    return promote_rule(S,T)
else
    error("no promotion exists")
end

convert and promote_rule are implemented for each type. Two such definitions for the
Complex128 type are:

promote_rule(::Type{Complex128},
    ::Type{Float64}) = Complex128
convert(::Type{Complex128}, x::Real) =
    complex128(x, 0)

With these definitions in place, a function may gain generic promotion behavior by adding
the following kind of definition:

+(x::Number, y::Number) = +(promote(x,y)...)  

This means that, given two numeric arguments where no more specific definition matches,
promote the arguments and retry the operation (the ... “splices” the two values returned by
promote into the argument list). The standard library contains such definitions for all basic
arithmetic operators. For this recursion to terminate, we require only that each Number type
implement + for two arguments of that type, e.g.

+(x::Int64, y::Int64) = ...
+(x::Float64, y::Float64) = ...
+(x::Complex128, y::Complex128) = ...

Therefore, each new type requires only one definition of each operator, and a handful of
convert and promote_rule definitions. If n is the number of types and m is the number of
operators, a new type requires \( O(n + m) \) rather than \( O(n \cdot m) \) definitions.

The reader will notice that uses of this mechanism involve multiple method calls, as well
as potentially expensive features such as tuple allocation and argument splicing. Without
a sufficient optimizing compiler, this implementation would be completely impractical. Fortunately,
through type analysis, inlining, elision of unnecessary tuples, and lowering of the
apply operation implied by ..., Julia's compiler is able to eliminate all of the overhead in
most cases, ultimately yielding a sequence of machine instructions comparable to that emitted
by a traditional compiler.

The most troublesome function is promote_type. For good performance, we must elide
calls to it, but doing so may be incorrect since the function might throw an error. By fortunate
coincidence though, the logic in promote_type exactly mirrors the analysis done by type
inference: it only throws an error if no matching methods exist for its calls to promote_rule,
in which case type inference concludes that the function throws an error regardless of which
Figure 1: Microbenchmark results (times relative to C++, log-scale). These measurements were carried out on a MacBook Pro with a 2.53GHz Intel Core 2 Duo CPU and 8GB of 1066MHz DDR3 RAM. The following versions were used: Python 2.7.1, MATLAB\textsuperscript{\textregistered} R2011a, Octave 3.4, R 2.14.2, V8 3.6.6.11. The C++ baseline was compiled by GCC 4.2.1, taking best timing from all optimization levels. Native implementations of array operations, matrix multiplication, sorting, are used where available.

4.2 Code Generation and Staged Functions

The presence of types and an inference pass creates a new, intermediate translation stage which may be customized (macros essentially customize syntax processing, and object systems customize run time behavior). This is the stage at which types are known, and it exists in Julia via the compiler’s method specialization machinery. Specialization may occur at run time during dispatch, or at compile time when inference is able to determine argument types accurately. Running custom code at this stage has two tremendous effects: first, optimized code can be generated for special cases, and second, the type inference system can effectively be extended to be able to make new type deductions relevant to the user’s application.

For example, we might want to write functions that apply to two arrays of different dimensionality, where the result has the higher of the two argument dimensionalities. One such function is a “broadcasting” binary elementwise operator, that performs computations such as adding a column vector to every column of a matrix, or adding a plane to every slice of a 3-dimensional dataset. We can determine the shape of the result array with the following function:

\begin{verbatim}
function promote_shape(s1::Tuple, s2::Tuple)
end
\end{verbatim}
if length(s1) > length(s2)
    return s1
else
    return s2
end
end

The type system can easily express the types of array shapes, for example (Int,Int) and (Int,Int,Int). However, inferring a sharp result type for this simple function is still challenging. The inference algorithm would have to possess a theory of the length and > functions, which is not easily done given that all Julia functions may be redefined and overloaded with arbitrary methods.

Instead, this function can be written as a staged function (or more accurately in our case, a staged method). This is a function that runs at an earlier translation “stage”, i.e. compile time, and instead of returning a result value returns code that will compute the result value when executed [19]. Here is the staged version of promote_shape:

```
@staged function promote_shape(s1::Tuple, s2::Tuple)
    if length(s1) > length(s2)
        quote return s1 end
    else
        quote return s2 end
    end
end
```

The signature of this definition behaves exactly like any other method signature: the type annotations denote run-time types for which the definition is applicable. However, the body of the method will be invoked on the types of the arguments rather than actual arguments, and the result of the body will be used to generate a new, more specialized definition. For example, given arguments of types (Int,Int) and (Int,Int,Int) the generated definition would be:

```
function promote_shape(s1::(Int,Int),
                      s2::(Int,Int,Int))
    return s2
end
```

Observe that the type of this function is trivial to infer.

The staged function body runs as normal user code, so whatever definition of > is visible will be used, and the compiler does not have to know how it behaves. Critically, the staged version of the function looks similar to the normal version, requiring only the insertion of `quote` to mark expressions deferred to the next stage.

In the case where a program is already statically-typeable, staged functions preserve that property. The types of the arguments to the staged function will be known at compile time, so the custom code generator can be invoked at compile time. Then the compiler may inline the result or emit a direct call to the generated code, as usual.

---

4The `@` denotes a macro invocation. At present, staged methods are implemented by a macro, but full integration into the language is planned.
Or, if the user does not require static compilation, the custom code generator can be invoked at run time. Its results are cached for each new combination of argument types, so compilation pauses are infrequent.

As a result, functions with complex type behavior can be implemented in libraries without losing performance. Of course, ordinary Julia functions may also have complex type behavior, and it is up to the library designer to decide which functions should be staged.

5 Evaluation

To evaluate Julia’s performance, we have compared its speed to that of six other languages: C++, Python, MATLAB®, Octave, R, and JavaScript. Figure 1 shows timings for five scalar microbenchmarks, and two simple array benchmarks; the same data are presented in tabular format in Table 1. All numbers are ratios relative to the time taken by C++.

MATLAB® has a JIT compiler that works quite well in some cases, but is inconsistent, and performs especially poorly on user-level function calls. The V8 JavaScript JIT compiler’s performance is impressive. Anomalously, both Julia and JavaScript seem to beat C++ on pi_sum, but we have not yet discovered why this might be.

The rand_mat_stat code manipulates many 5-by-5 matrices. Here the performance gaps close, but the arrays are not large enough for library time to dominate, so Julia’s ability to specialize call sites wins the day (despite the fact that most of the array library functions involved are written in Julia itself).

The rand_mat_mul code demonstrates a case where time spent in BLAS [22] dominates. MATLAB® gets its edge from using a multi-threaded BLAS (threading is available in the BLAS Julia uses, but it was disabled when these numbers were taken). R may not be using a well-tuned BLAS in this install; more efficient configurations are probably possible. JavaScript as typically deployed is not able to call the native BLAS code, but the V8 compiler’s work is respectable here.

Julia is not yet able to cache generated native code, and so incurs a startup time of about two seconds to compile basic library functions. For some applications this latency is a barrier to deployment, and we plan to address it in the future.

<table>
<thead>
<tr>
<th>test</th>
<th>Julia</th>
<th>Python</th>
<th>MATLAB®</th>
<th>Octave</th>
<th>R</th>
<th>JavaScript</th>
</tr>
</thead>
<tbody>
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<td>31.47</td>
<td>1336.37</td>
<td>2383.80</td>
<td>225.23</td>
<td>1.55</td>
</tr>
<tr>
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<td>16.50</td>
<td>815.19</td>
<td>6454.50</td>
<td>337.52</td>
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<tr>
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<td>55.84</td>
<td>132.71</td>
<td>3127.50</td>
<td>713.77</td>
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</tr>
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<td>mandel</td>
<td>5.55</td>
<td>31.15</td>
<td>65.44</td>
<td>824.68</td>
<td>156.68</td>
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</tr>
<tr>
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<td>18.03</td>
<td>1.08</td>
<td>328.33</td>
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<tr>
<td>rand_mat_stat</td>
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<td>39.34</td>
<td>11.64</td>
<td>54.54</td>
<td>22.07</td>
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<tr>
<td>rand_mat_mul</td>
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<td>1.18</td>
<td>0.70</td>
<td>1.65</td>
<td>8.64</td>
<td>41.79</td>
</tr>
</tbody>
</table>

Table 1: Microbenchmark results (times relative to C++).
5.1 Effectiveness of Specialization Heuristics

Given our implementation strategy, excessive compilation and corresponding memory use are potential performance concerns. We measured the number of method compilations performed both with and without our specialization heuristics, and the heuristics were able to elide about 12% of compilations. This is not a large fraction, but it is satisfying given that the heuristics can be computed easily, and only by manipulating types. On average, each method is compiled about 2.5 times.

Memory usage is not unreasonable for modern machines: on a 64-bit platform Julia uses about 50MB of memory on startup, and after loading several libraries and working for a while memory use tends to level off around 150-200MB. Pointer-heavy data structures consume a lot of space on 64-bit platforms. To mitigate this problem, we store ASTs and type information in a compact serialized format, and deserialize structures when the compiler needs them.

5.2 Effectiveness of Type Inference

It is interesting to count compiled expressions for which a concrete type can be inferred. In some sense, this tells us “how close” Julia is to being statically typed, though in our case this is a property of both the language implementation and the standard library. In a run of our test suite, code was generated for 135375 expressions. Of those, 84127 (62%) had a type more specific than Any. Of those, 80874 (96%) had a concrete static type.

This suggests that use of dynamic typing is fairly popular, even though we try to avoid it to some extent in the standard library. Still, more than half of our code is well-typed. The numbers also suggest that, despite careful use of a rich lattice, typing tends to be an all-or-nothing affair. But, it is difficult to estimate the effect of the 4% abstractly-typed expressions on the other 96%, not to mention the potential utility of abstract inferred types in code that was not actually compiled.

These numbers are somewhat inaccurate, as they include dead code, and it may be the case that better-typed methods tend to be recompiled with different frequency than others, biasing the numbers.

5.3 Productivity

Our implementation of Julia consists of 11000 lines of C, 4000 lines of C++, and 3500 lines of Scheme (here we are not counting code in external libraries such as BLAS and LAPACK). Thus we have significantly less low-level code to maintain than most scripting languages. Our standard library is roughly 25000 lines of Julia code. The standard library provides around 300 numerical functions of the sort found in all technical computing environments. We suspect that our library is one of the most compact implementations of this body of functionality.

At this time, every contributor except the core developers is a “new user” of Julia, having known of the language for no more than six months. Despite this, our function library has received several significant community contributions, and numerous smaller ones. We take this as encouraging evidence that Julia is productive and easy to learn.

6 Community

Julia is an open source project, with all code hosted on github [14]. It has attracted 550 mailing list subscribers, 1500 github followers, 190 forks, and more than 50 total contributors.
Text editor support has been implemented for emacs, vim, and textmate. Github recognizes Julia as the language of source files ending in .jl, and can syntax highlight Julia code listings.

Several community projects are underway: two plotting packages, interfaces to arbitrary-precision arithmetic library GMP, bit arrays, linear programming, image processing, polynomials, GPU code generation, a statistics library, and a web-based interactive environment. A package management framework will soon be in place.

We hope Julia is part of a new generation of dynamic languages that not only run faster, but foster more cooperation between the programmer and compiler, pushing the standard of productivity ever higher.

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References


